

1. Expand out the expression for the parallel transport matrix  $U$  and show that to second order in the size (typical width) of the loop, for a closed path,

$$U^\alpha{}_\beta = \delta^\alpha_\beta - \frac{1}{2} R^\alpha{}_{\beta\mu\nu} \mathcal{M}^{\mu\nu} + \dots$$

where

$$\mathcal{M}^{\mu\nu} = \oint x^\mu dx^\nu.$$

Show that  $\mathcal{M}^{\mu\nu}$  is antisymmetric. If the path is around a small parallelogram with sides given by tangent vectors  $A$  and  $B$ , show that  $\mathcal{M}^{\mu\nu} = A^\mu B^\nu - A^\nu B^\mu$ .